

#### WARP3D Implementation of MKL Cluster PARDISO Solver

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#### Overview



- WARP3D Overview
- Experiments and results for MKL PARDISO driver
- Experiments and results with WARP3D
- Conclusion

#### WARP3D



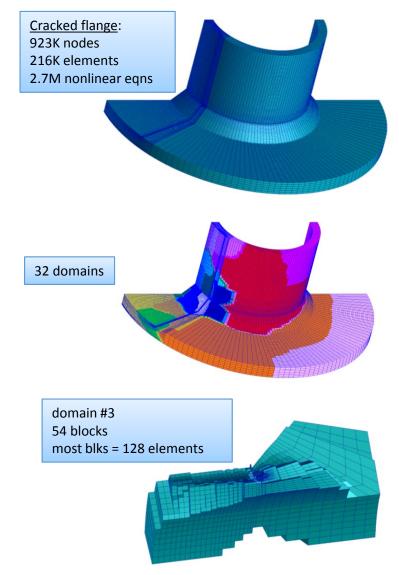
- Open-source code for nonlinear analysis of 3D solids using finite elements
- Primary applications: design, safety, life extension in heavy energy production systems
- Code extensively developed for 20 years in university
- Linux, Windows, Mac OS using Intel software tools
- Works with the iterative solver HYPRE and direct solver MKL Cluster PARDISO
- ~175K lines of code (Fortran 90-2008)

 $\underline{www.warp3d.net} \rightarrow \text{documentation, ready-to-run executables, verification/example suites}$  $\underline{www.github.com/rhdodds/warp3d} \rightarrow \text{source code}$ 



#### Parallel Architecture

- FE mesh partitioned into domains then blocks of elements
- Domain # = MPI rank, > 1 thread per rank
- # elements per block tuned to # vector registers & cache architecture
- A thread (OpenMP) processes all computations for entire block
- Vectorization within each thread runs inner loops on # elements per block
- Structure of Arrays (SoA) design





#### Background on MKL PARDISO

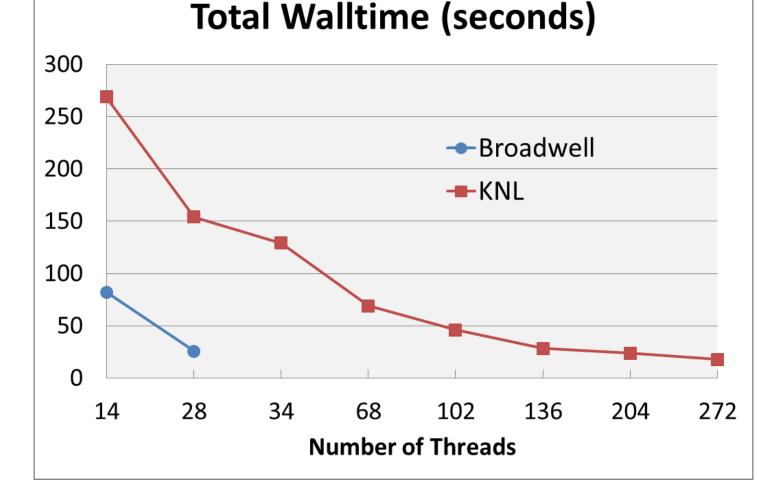
- MKL PARDISO is a Parallel, Direct Sparse Matrix Solver
  - Cluster MKL hybrid MPI/OpenMP implementation
- MKL PARDISO can account for 80-95% of total run time in WARP3D for large models
- Primary impact for WARP3D is **factorization time** 
  - Algorithm based on Level-3 BLAS and using a combination of leftand right-looking supernode techniques
  - Called by WARP3D thousands of times per simulation
  - Sparsity structure of the matrix is fixed for a given simulation, with coefficients changing over simulation time



#### MKL PARDISO Driver

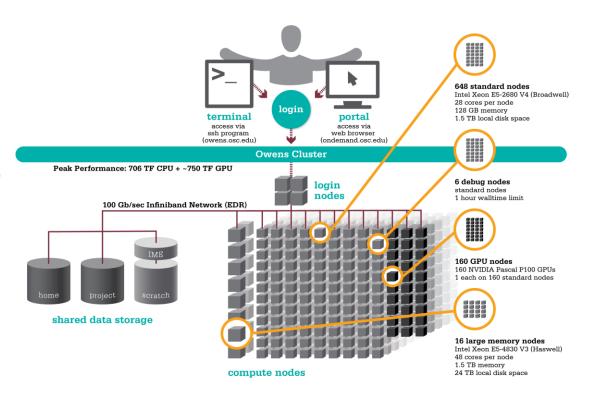
#### Model

- 1.4M equations, symm. pos. definite
- 10.5 TFlop for factorization
- 20 GB memory used for factorization
- Benchmarking on
  - Intel Broadwell (OSC Owens)
  - Intel KNL (TACC Stampede 1.5)
- KNL performs as well as Broadwell when utilizing all the threads



# Intel Broadwell Environment

- Ohio Supercomputer Center (Owens Cluster)
- Node Description
  - Dell PowerEdge C6320 two-socket servers
  - Intel Xeon E5-2680 v4 (Broadwell, 14 cores, 2.40 GHz)
  - 128 GB Memory
- Mellanox EDR (100 Gbps) Infiniband networking
  - MPI Fabric: DAPL
  - I\_MPI\_DAPL\_TRANSLATION\_CACHE=0\*
- Uses Intel 17.0.2 and Intel MPI 2017.2



\* https://software.intel.com/en-us/forums/intel-clusters-and-hpc-technology/topic/737528



## Intel KNL Environment

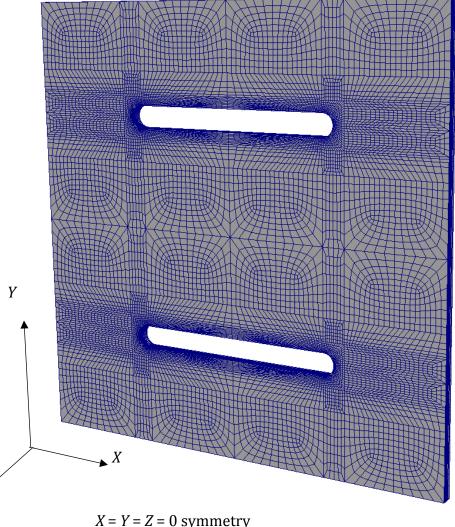
- Texas Advanced Computing Center (Stampede2 Cluster)
- Node Description
  - Single-socket servers
  - Intel Xeon Phi 7250 (KNL, 68 cores, 1.40 GHz)
  - 96 GB DDR4 Memory + 16 GB MCDRAM
- Intel Omni-Path (100 Gbps) networking
  - MPI Fabric: TMI
- Memory/Cluster Modes Benchmarked
  - Cache Quadrant Mode
  - Flat Quadrant Mode prefer MCDRAM
- Uses Intel 17.0.4 and Intel MPI 17.0.3





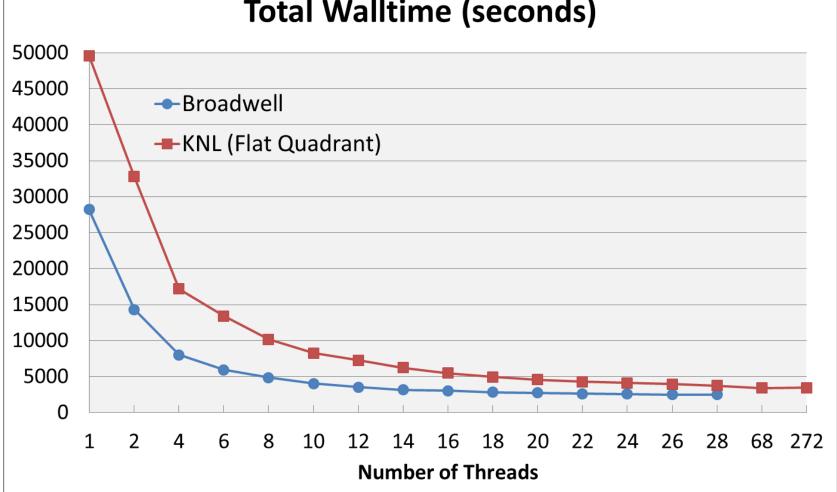
#### Finite Element Model

- Large plate-like structure with multiple holes
- 924,999 nodes
- 218,240 elements
- 2.73M equations
  - 52.7 TFlop for factorization
  - ~62 GB memory used for factorization
- 20-node elements
- Tension loading
- 5 load(time) steps that cause moderate yielding



# Single Node Performance

- PARDISO takes 95-99% of total run time in WARP3D
- Best Broadwell is **1.37**x faster than best KNL timing
- 20 threads for Broadwell and 26 threads for KNL are converged to within 10% of best timings
- Unable to run single-node • Cache Quadrant mode on KNL due to memory issue

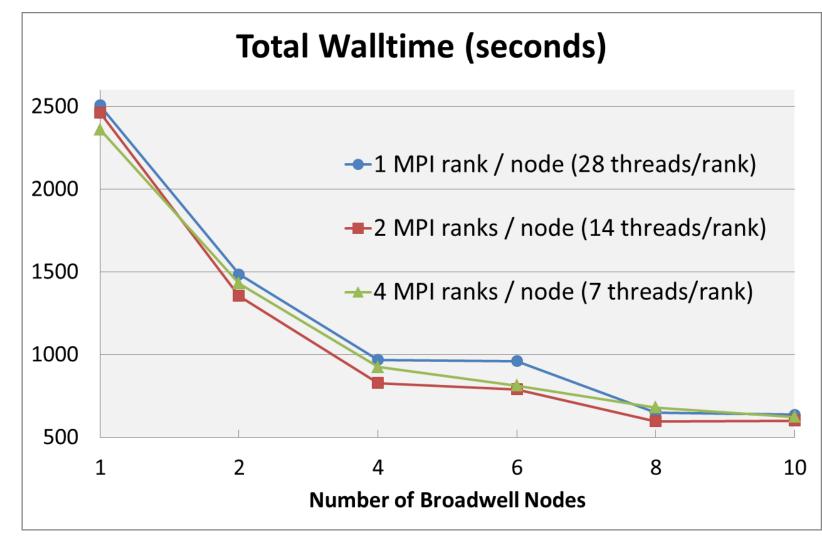


Total Walltime (seconds)

## Intel Broadwell MPI



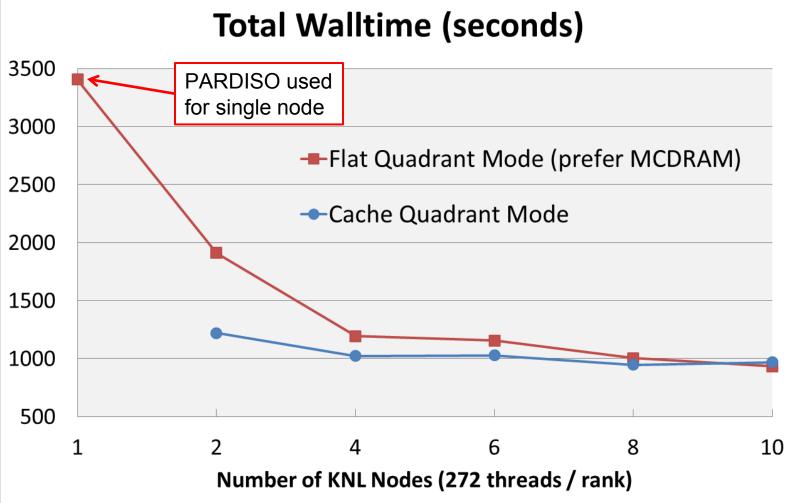
- Cluster PARDISO takes 83-96% of total run time in WARP3D
- Observed 1.06x speedup on single node when using 4 MPI processes
- For >1 node, best performance using 1 MPI rank per socket (2 MPI rank / node)
- Little improvement beyond 8 nodes (4.1x speedup for 2 MPI rank / node)



## Intel KNL MPI



- Cluster PARDISO takes 73-96% of total run time in WARP3D
- Memory issue observed for Cache mode on single node
- Cache mode is 1.56x faster than Flat mode for 2 nodes and quickly converge for more nodes
- Little improvement beyond 8 nodes (3.4x speedup for Flat mode)



#### Conclusions and Insights

- Broadwell performs 1.37x faster than KNL on a single node (Flat mode)
- Best parallel performance observed when running a single MPI process per socket for dual-socket Broadwell
- Cache mode outperforms Flat mode for multi-node, but rapidly converges as more nodes are added
- Need to investigate distributed assembly option in WARP3D for Cluster PARDISO

Supported by the Intel<sup>®</sup> Parallel Computing Center at the Ohio Supercomputer Center and Texas Advanced Computing Center.



## HYPRE Comparison

- Benchmarked on Intel Broadwell (16 Nodes)
- Solvers
  - Cluster PARDISO
  - HYPRE parallel assembly across nodes
  - HYPRE element stiffnesses computed on ranks, moved to root, assembled, hypre called
- HYPRE performance improves with less strict tolerance even when number of global Newton iterations increases from 16 → 18
- Need to investigate conversion to CSR for HYPRE with parallel assembly off (took 109 seconds)
- Need to investigate distributed assembly option for Cluster PARDISO

	Tolerance	Total Walltime (s)	Eqn Solves
Cluster PARDISO	N/A	516	16
HYPRE (Parallel Assembly)	1.00E-5	722	16
	1.00E-4	597	16
	1.00E-3	484	16
	1.00E-2	374	16
	1.00E-1	323	18
HYPRE (Assembly on root node)	1.00E-1	421	18