

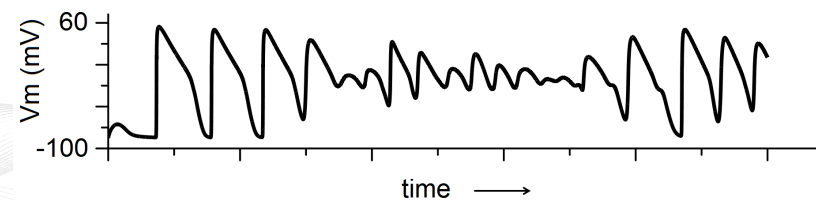
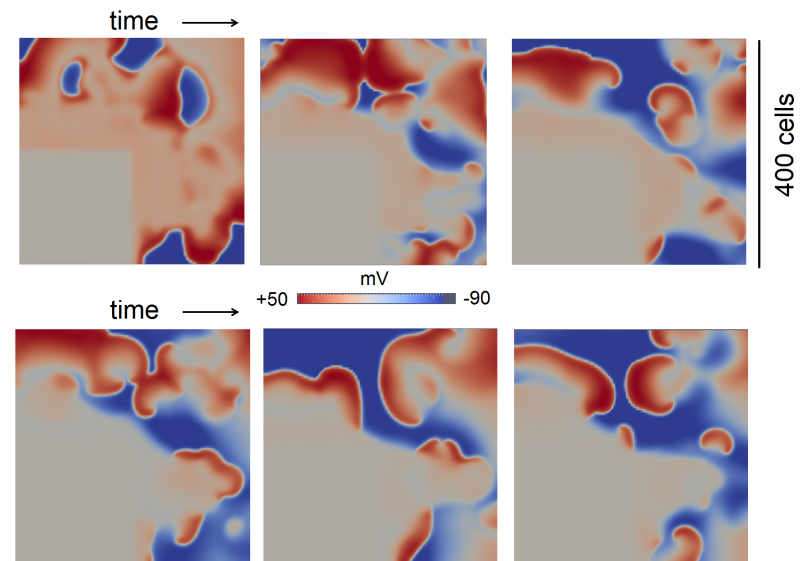
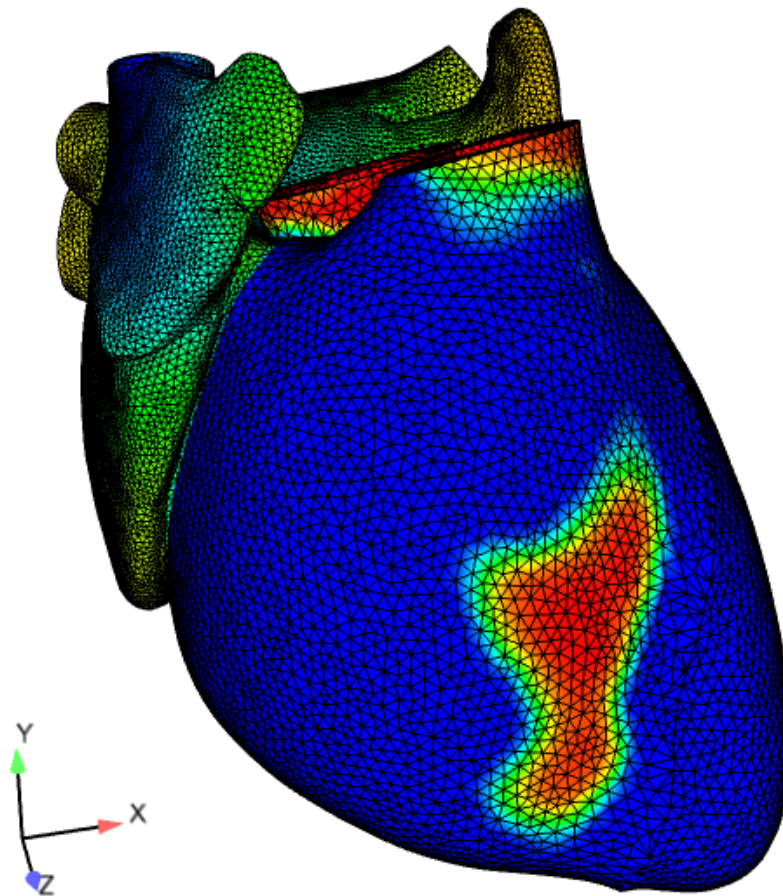
Porting Tissue-scale Cardiac Simulations to the Knights Landing Platform

Johannes Langguth

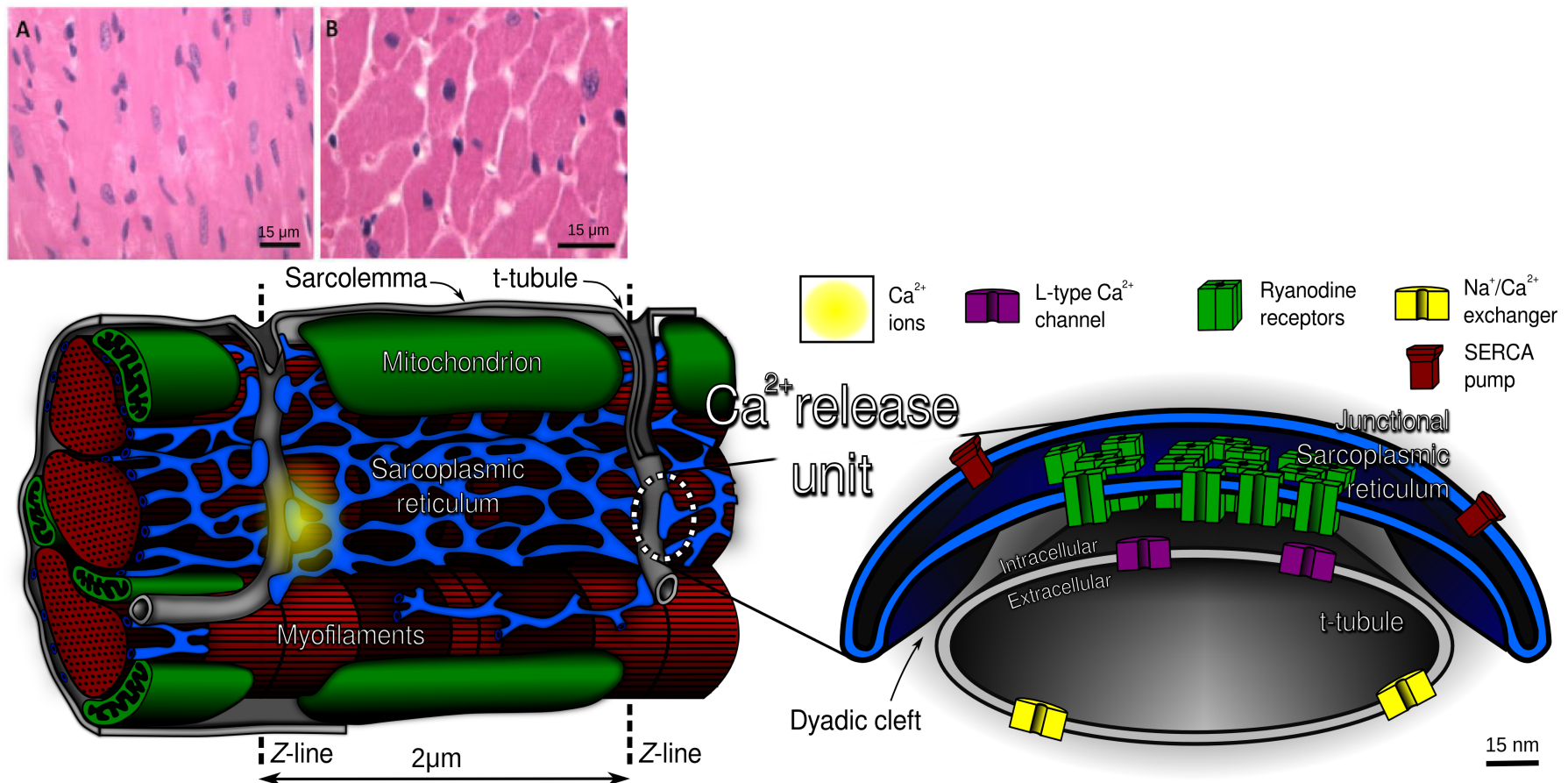
Simula Research Laboratory, Oslo, Norway

joint work with
Chad Jarvis and Xing Cai

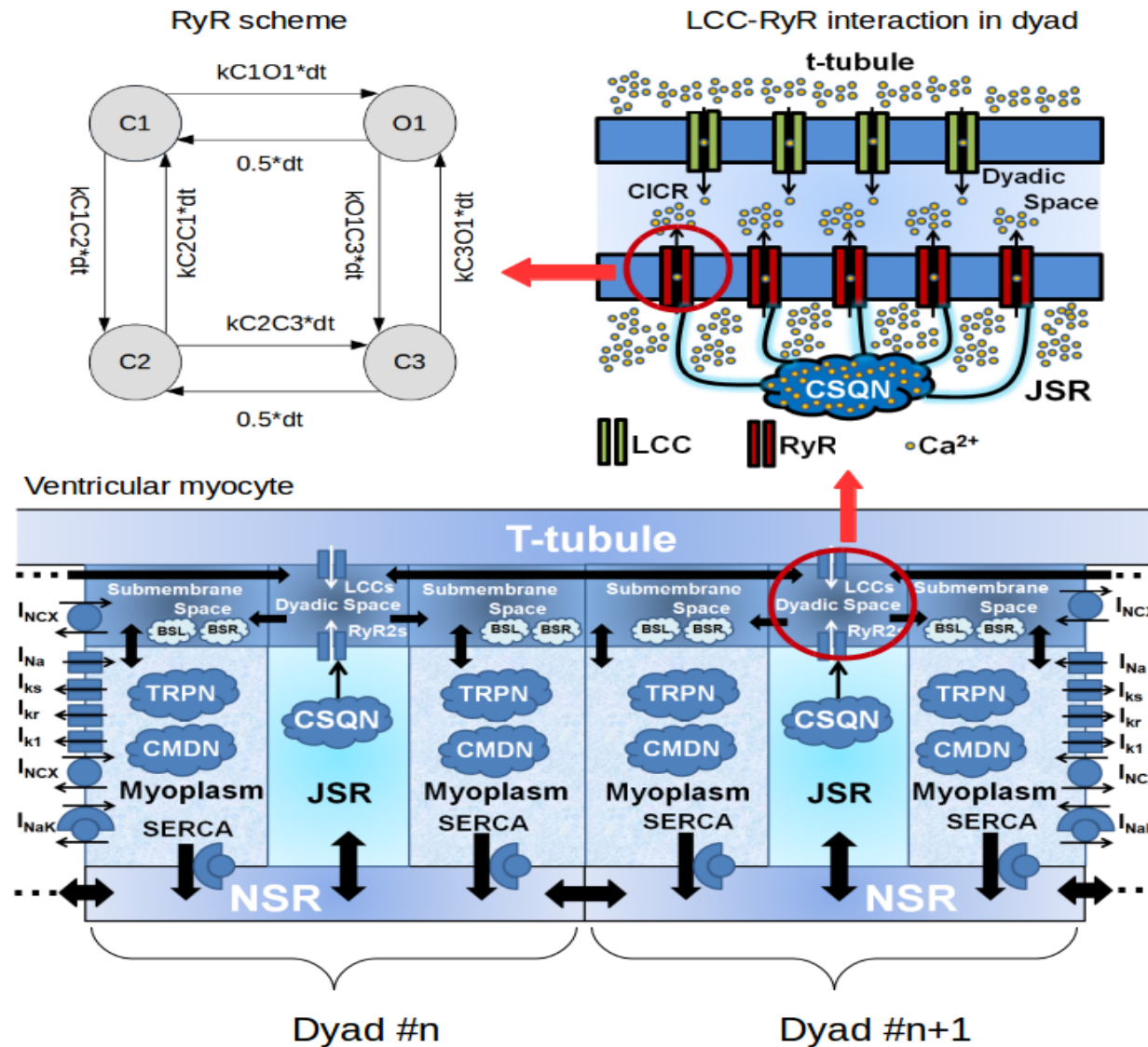
Cardiac Electrophysiology



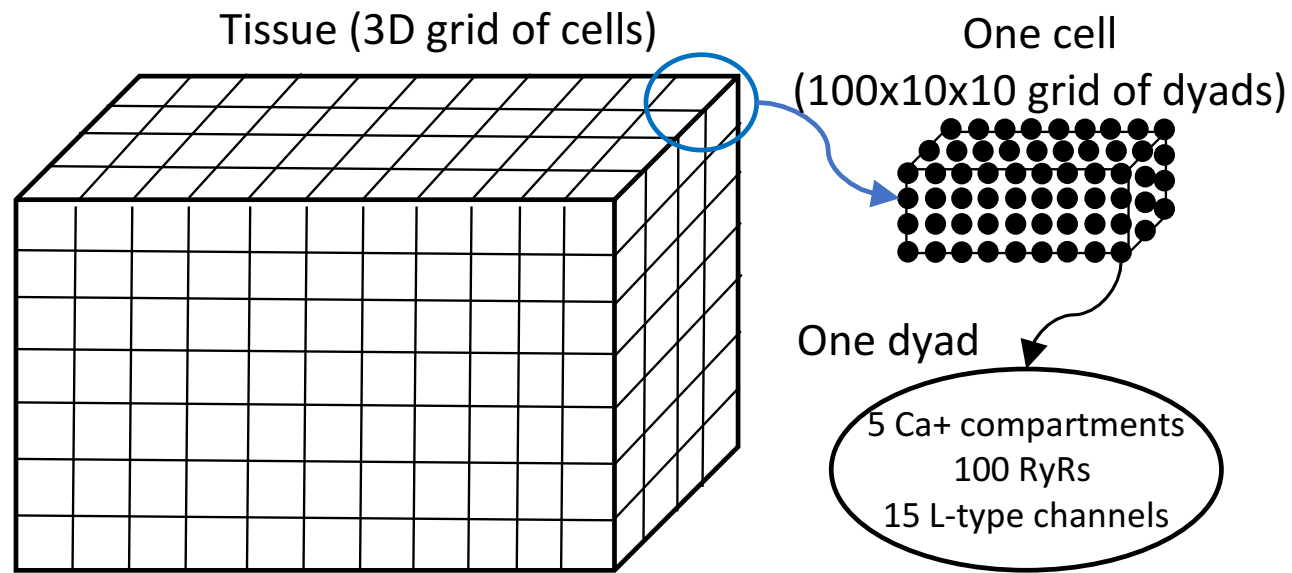
Calcium Handling in the Human Cardiac Ventricle



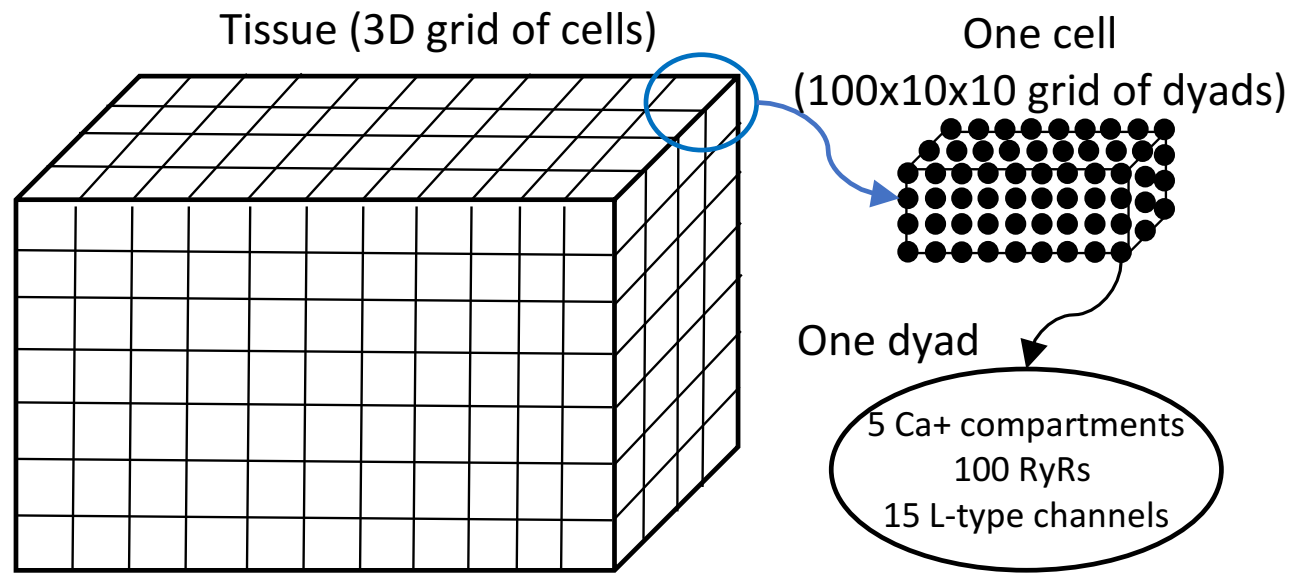
Ryanodine Receptors



Computational Scope



Computational Scope



- $2 * 10^9$ Cells in the heart
- 10^4 Dyads per cell
- 10^2 Ryanodine Receptors (RyRs) per dyad
- 10^4 Time steps per heartbeat

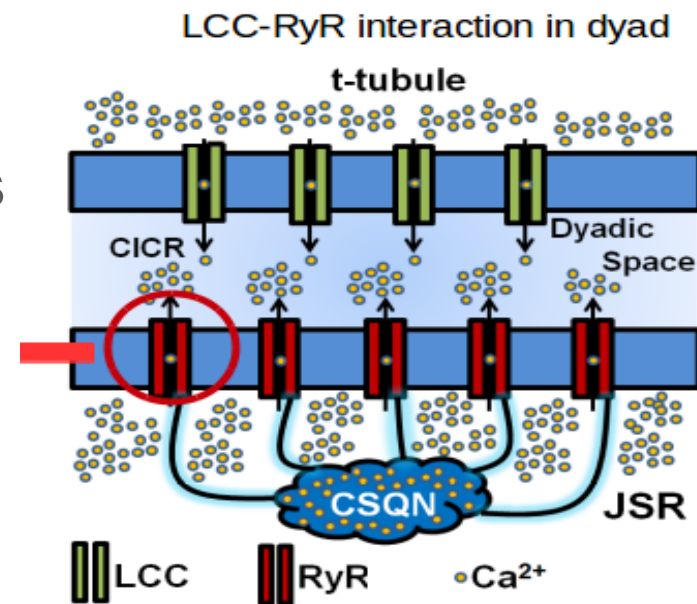
10^{19} possible state transitions

Computation Timestep

For each Cell do (OpenMP parallel for)

1. Compute L-type opening probabilities
2. Simulate L-type opening
3. Compute RyR opening probabilities
4. Simulate RyR opening
5. Compute calcium concentrations
6. Dyad diffusion

Cell diffusion (Local & MPI)



Computation Timestep

For each Cell do (OpenMP parallel for)

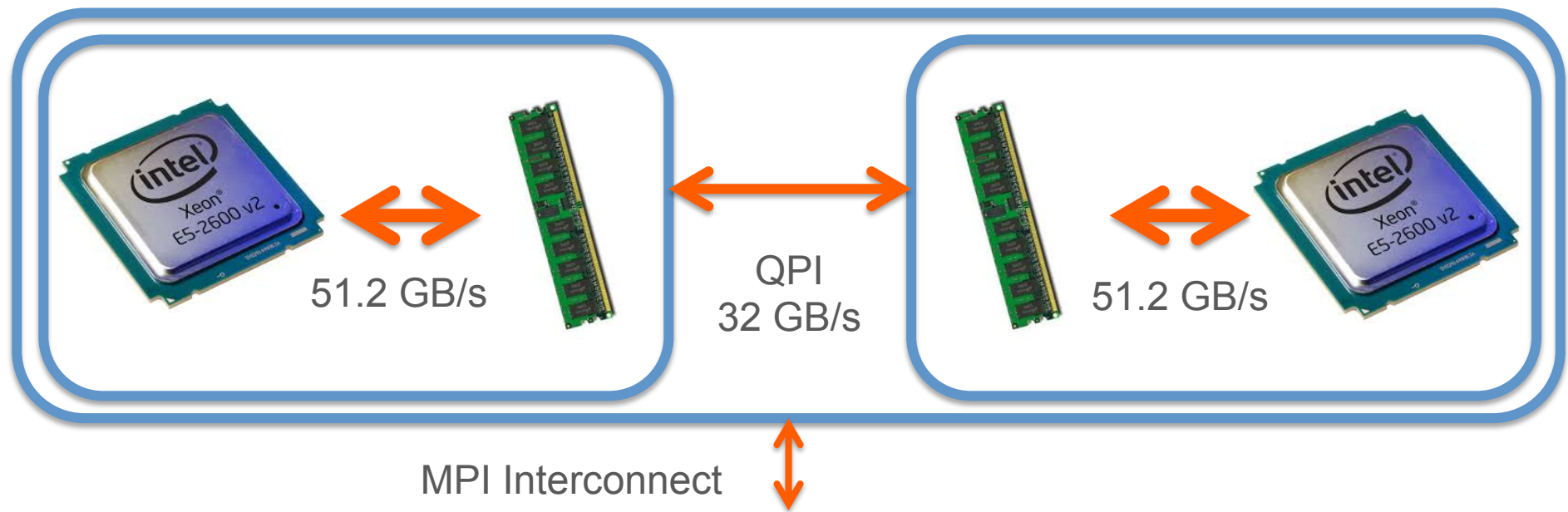
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Cell diffusion (Local & MPI)

Relevant metric: Cell computations/s (CC/s)

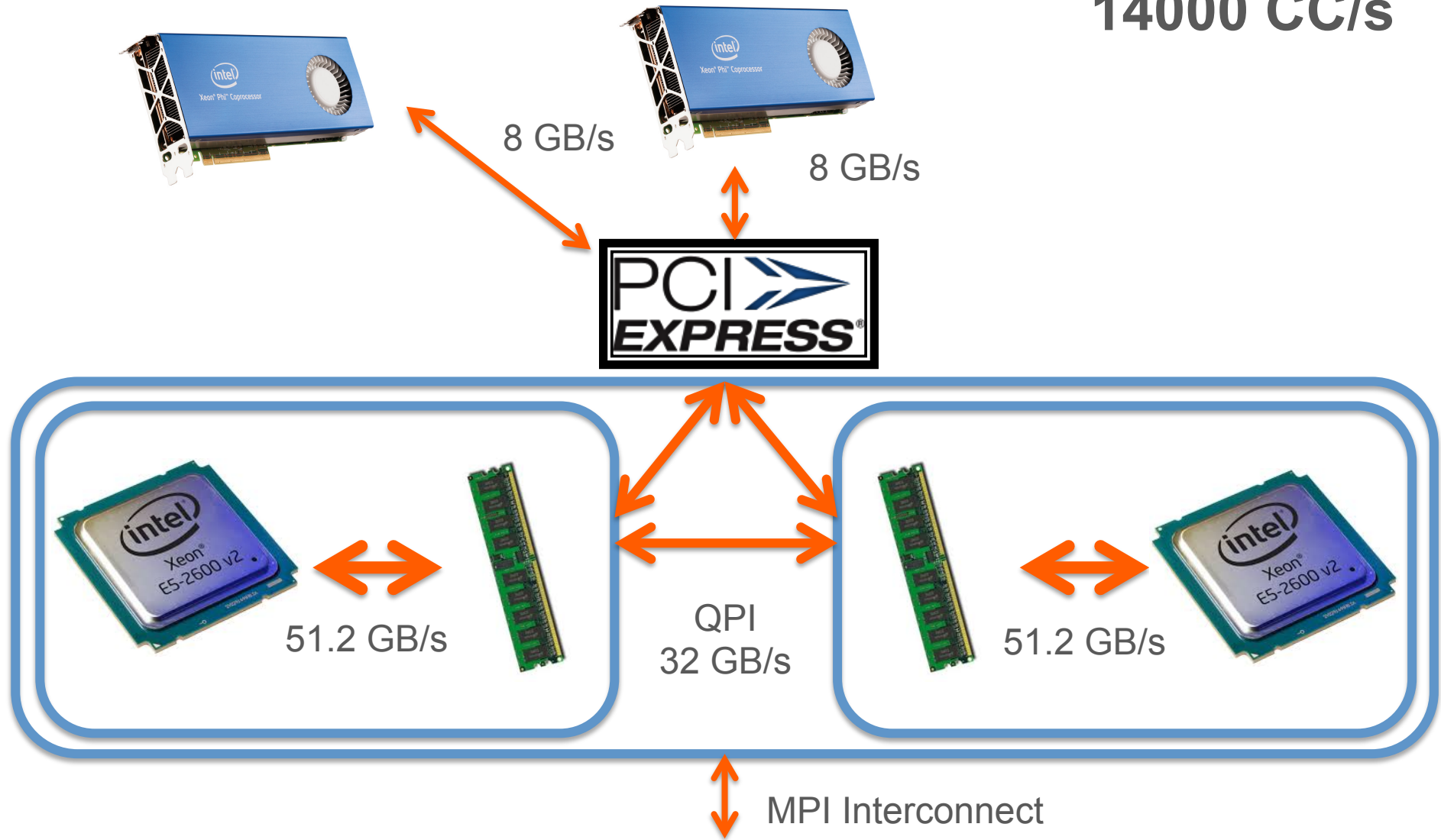
Basic Configuration: Dual Sandy Bridge

4000 CC/s
(Cell computations
per second)



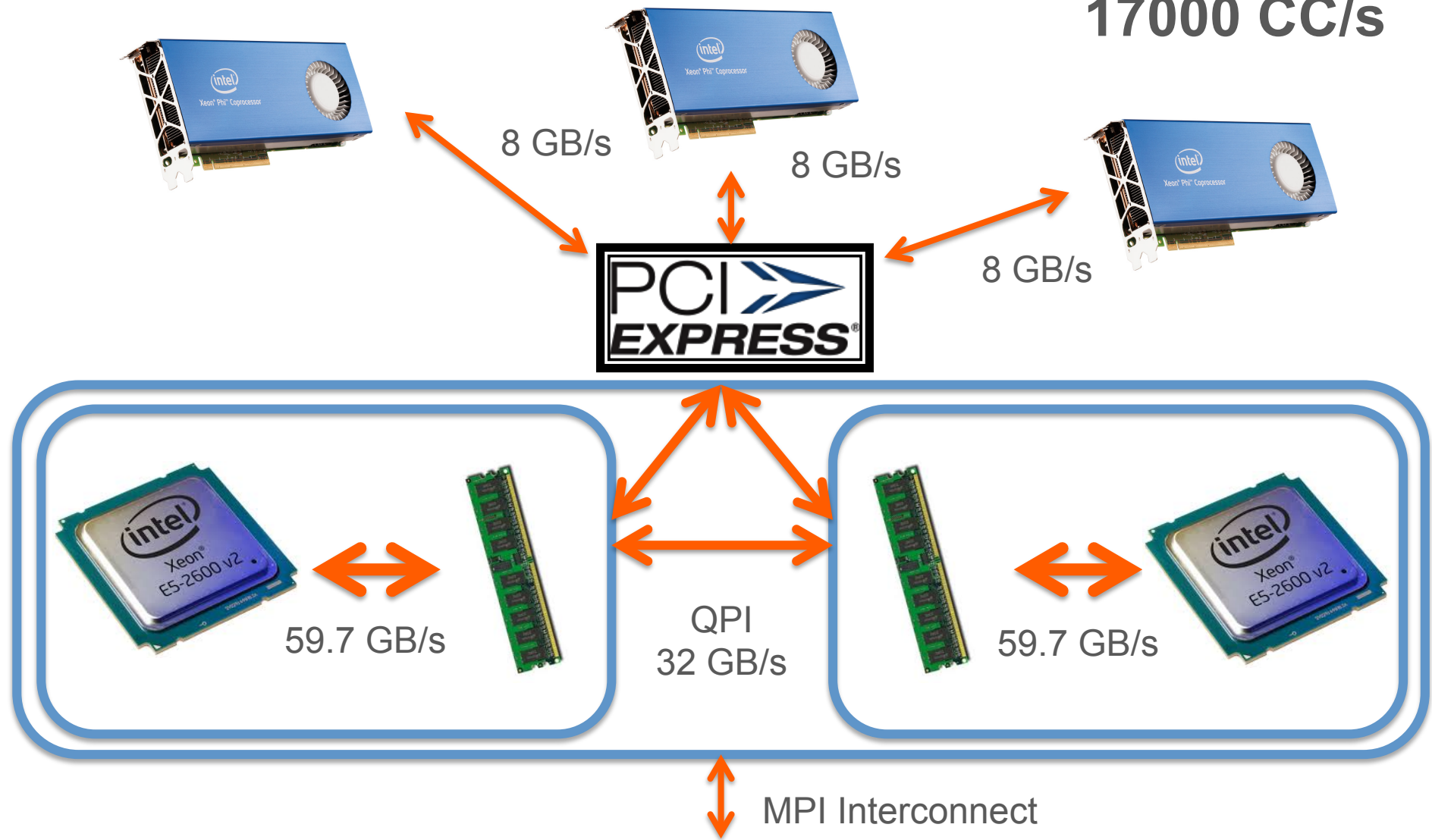
Node Structure on Abel

14000 CC/s



Node Structure on TianHe-2

17000 CC/s

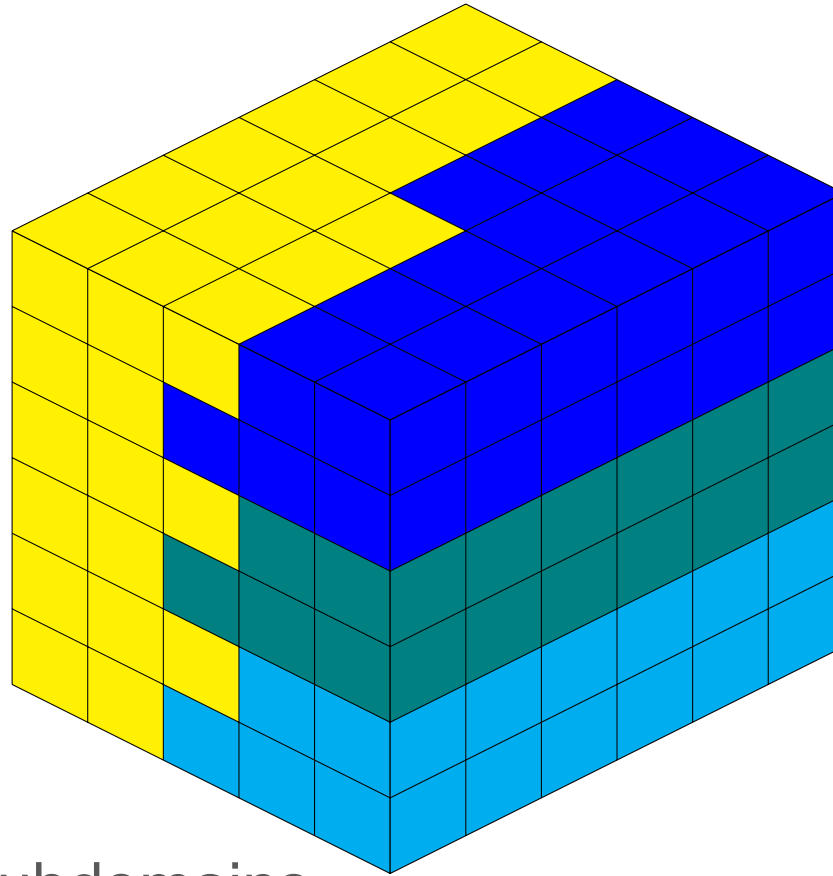


Computation on TianHe-2



- Largest grid so far: 3.2 million (400 nodes)
- Problem: heterogeneous load balancing and memory
- Need about 3 MB per cell -> about 2000 cells per Phi max
- Find feasible and balanced allocation to avoid idling

Domain Decomposition



- Cuboid node subdomains
- Unstructured intra-node subdomains
- Use 20 x 20 x 20 node subdomains
- 93% CPU load

Xeon Phi 7250 Server



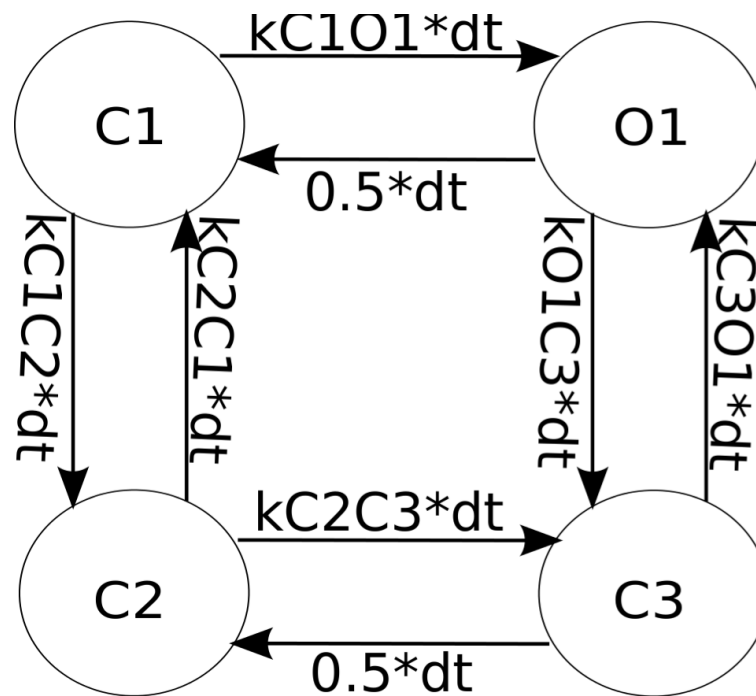
14000 CC/s
“Out of the box”

- **16 GB MCDRAM**
- **96 GB DDR4**
- **Homogeneous**

- **5000 Cells in HBM**
- **34000 Cells in DDR4**

State Transitions

- Stochastic state transitions for each ryanodine receptor
- 10^6 possible state transitions per cell and time step
- Bernoulli trials (coin toss) cost too many random numbers
- Binomial distributions are efficient but irregular
- Difficult vectorization due to variable number of RyRs per state

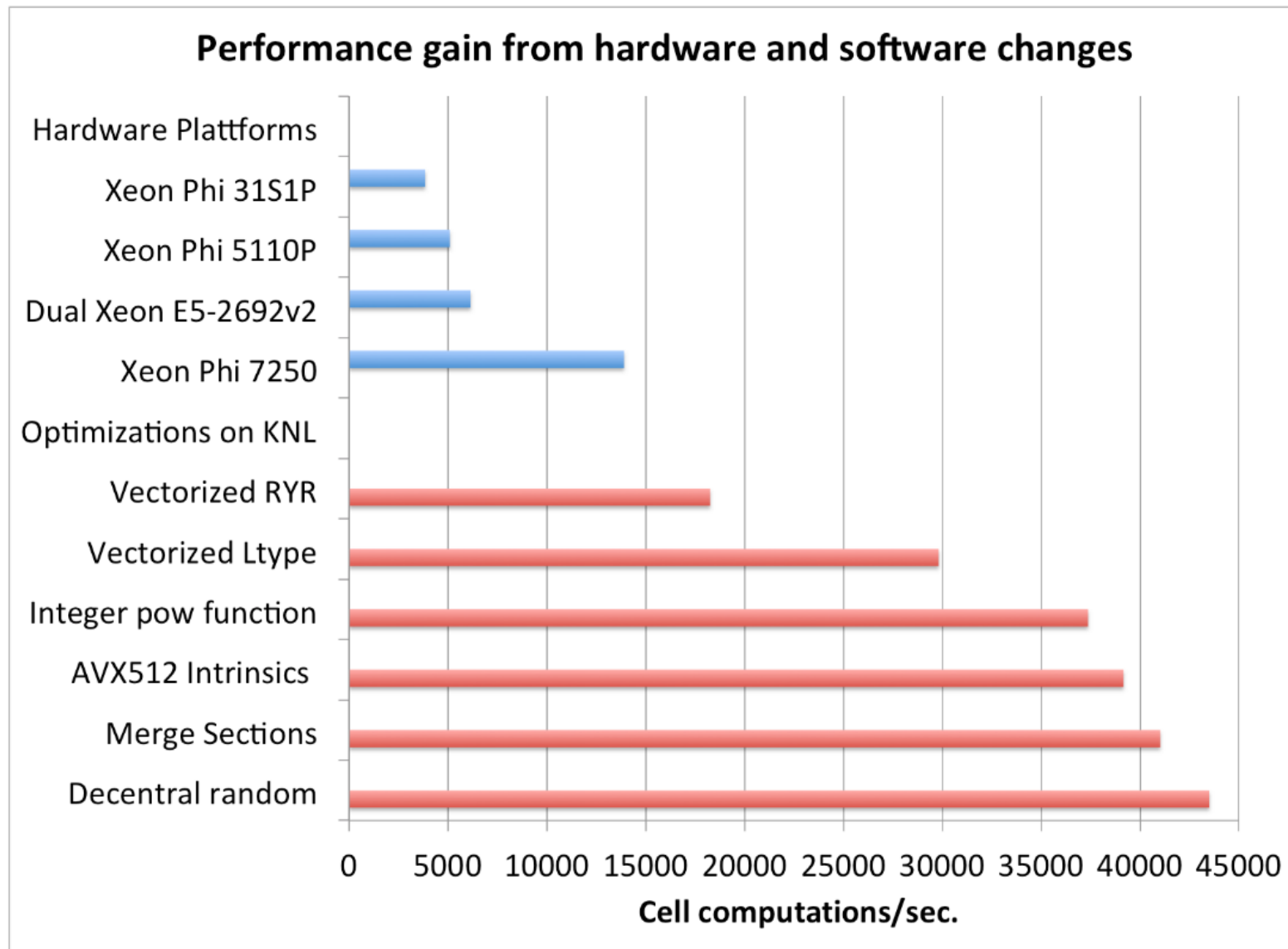


Vectorized Binomial Distribution Sampling

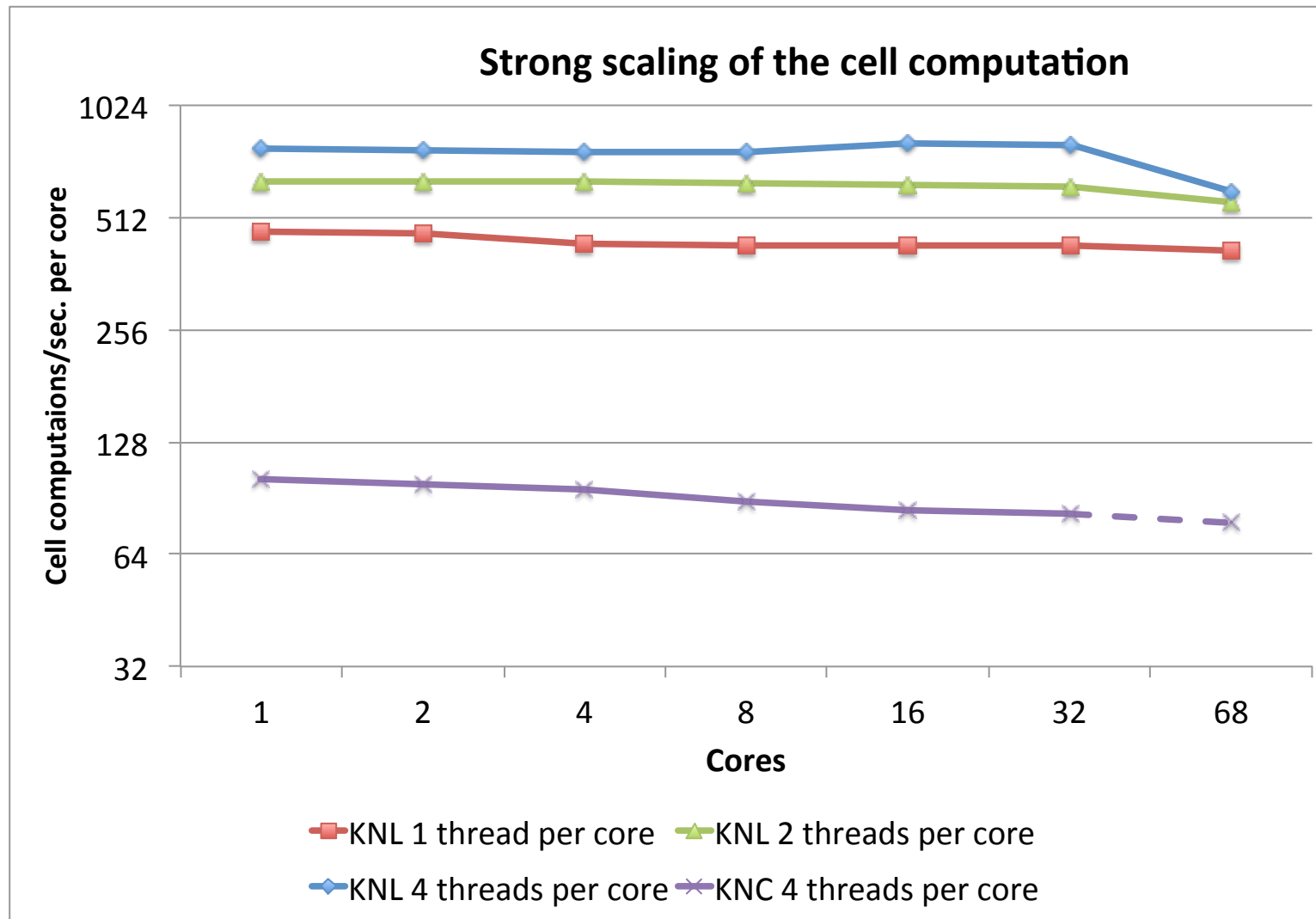
$$F(k; n, p) = \Pr(X \leq k) = \sum_{i=0}^{\lfloor k \rfloor} \binom{n}{i} p^i (1-p)^{n-i}$$

```
function VectorizedBinomial {  
    Input: Vectors N, P, RANDVAL  
    Output: Vector K  
    Initialize K = 0  
    Initialize 1P = Vector_subtract(1,P);  
    Initialize PKNK = Vector_power(1P,N);  
    Initialize P1P = Vector_divide(P,1P);  
    for (int i = 0; i < max(N); i++) {  
        BC = Vector_gather(BC_table,N,K);  
        SUB = Vector_multiply(BC,PKNK);  
        RANDVAL = Vector_subtract(RANDVAL,SUB);  
        PKNK = Vector_multiply(P1P,PKNK);  
        MASK = Vector_mask_compare(MASK,RANDVAL > 0);  
        K = Vector_mask_add(K,1,MASK);  
    }  
}
```

Performance Improvement



Strong Scaling



Hyperthreading matters, bandwidth limited

Memory Strategies

1. Cache Mode

- Easiest to use
- Loss of memory

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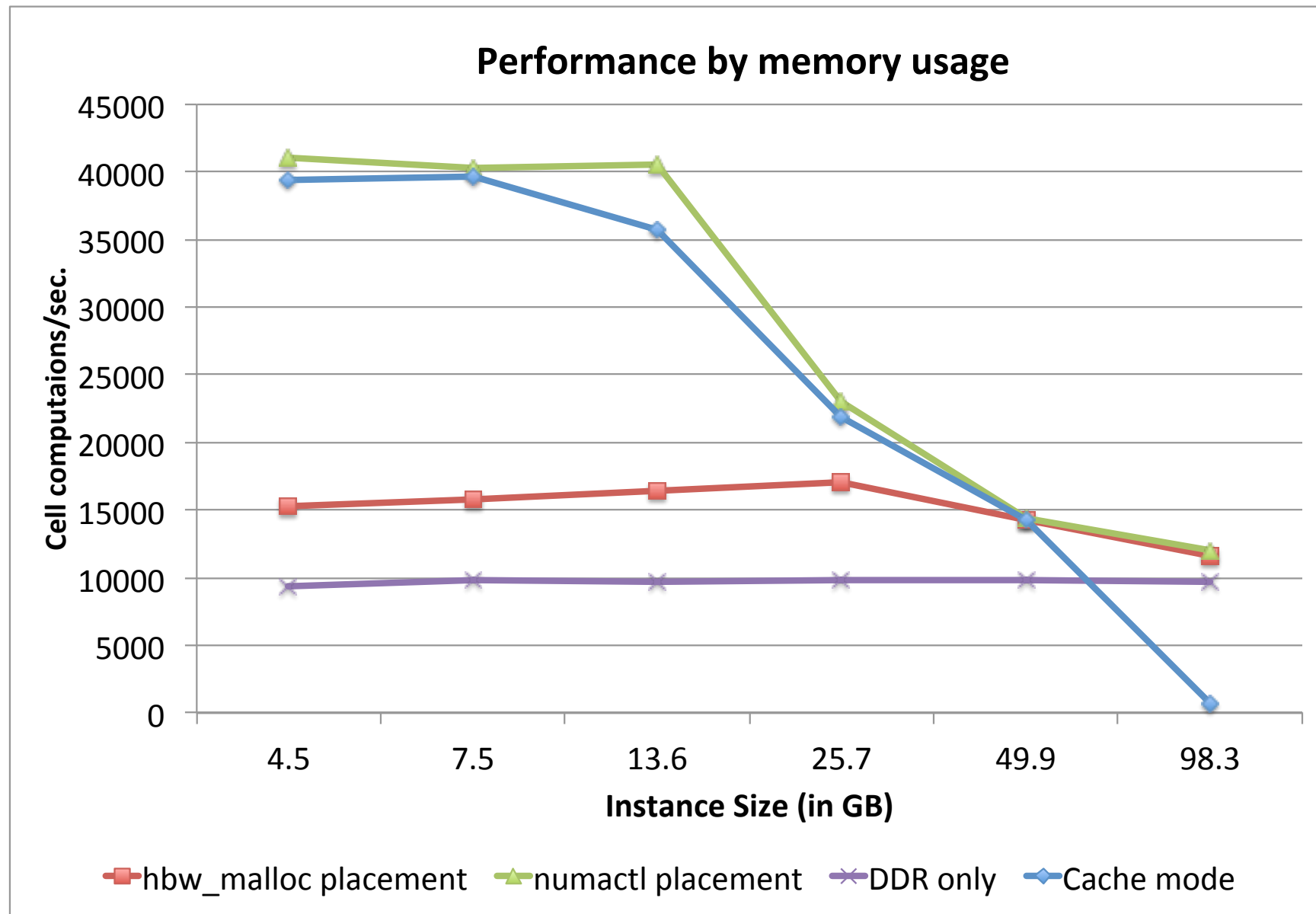
2. Flat mode with *hbwallocl*

- Maximum control
- Size specific

3. Flat mode with ordering and *numactl -preferred=1*

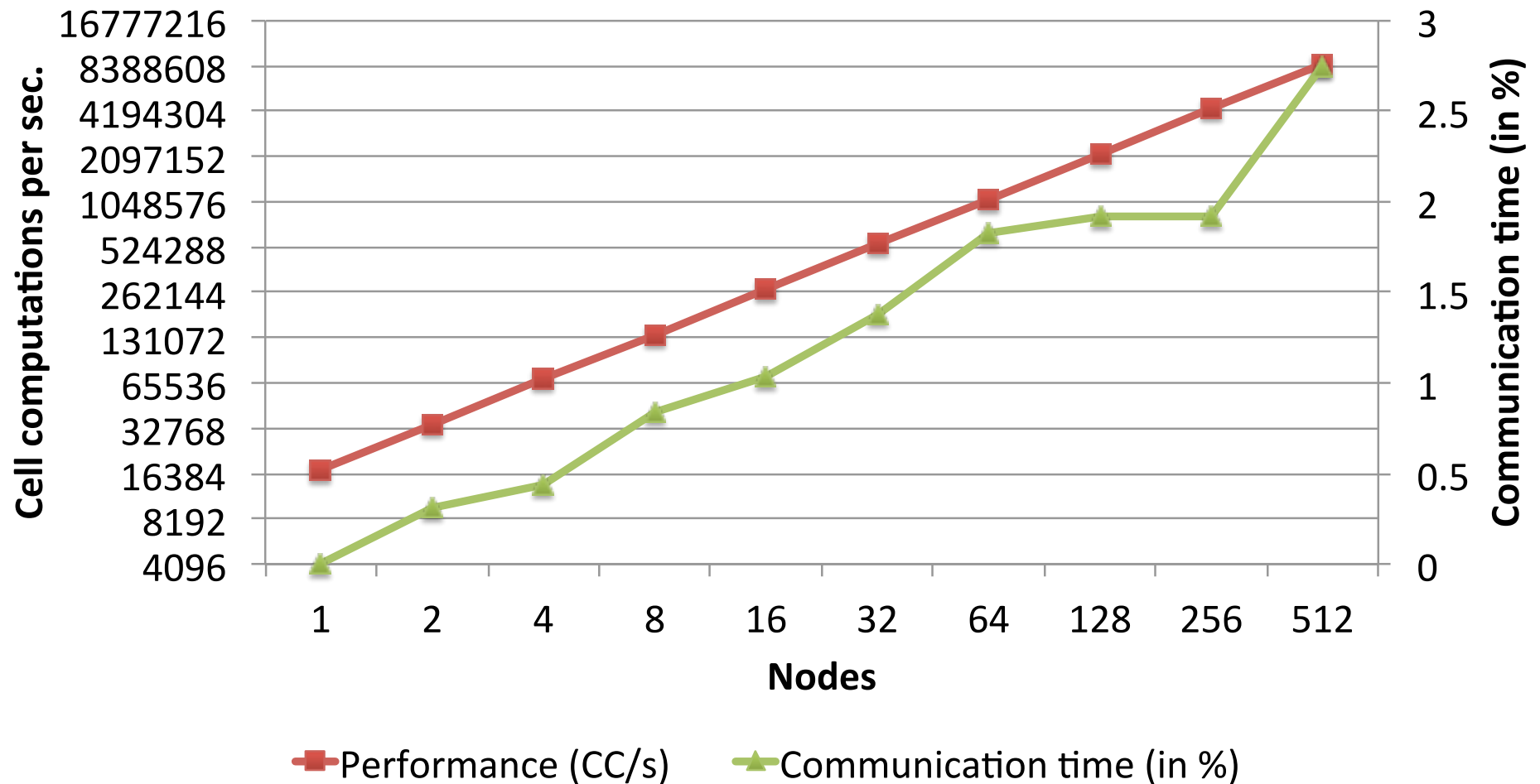
- Easy and portable
- Software development hazard

Performance is Memory Dependent

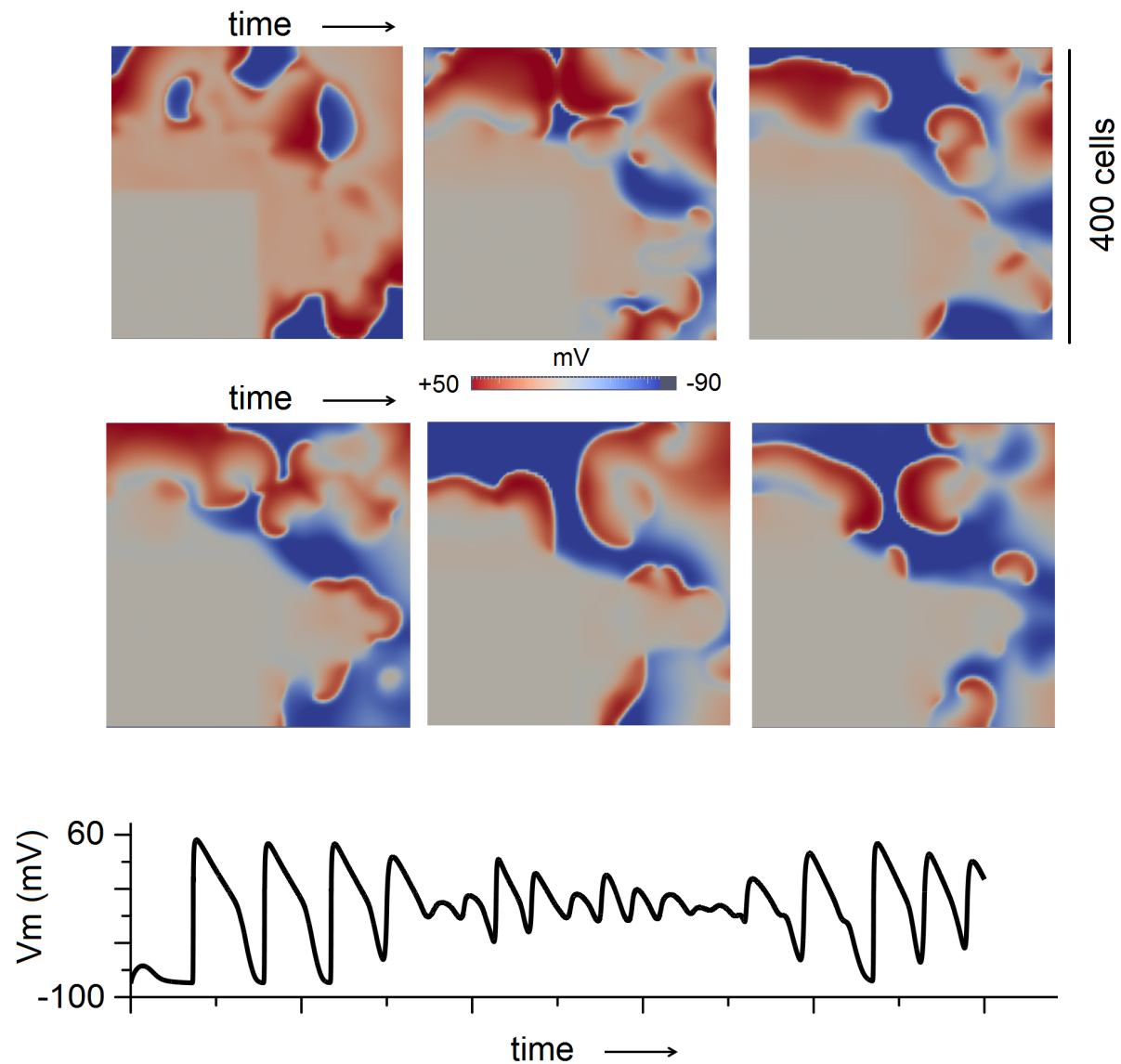


Scaling is not a Problem (on TH-2)

Weak scaling of the heterogeneous computation



Simulation of Unhealthy Tissue



Observations

- Difficult computation
- Easy communication
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- KNL has decent performance “for free” (3x over KNC)
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- K20X GPU delivers $\frac{1}{2}$ KNL CC/s @ $\frac{1}{2}$ KNL GB/s
- P100 and V100 could be much faster

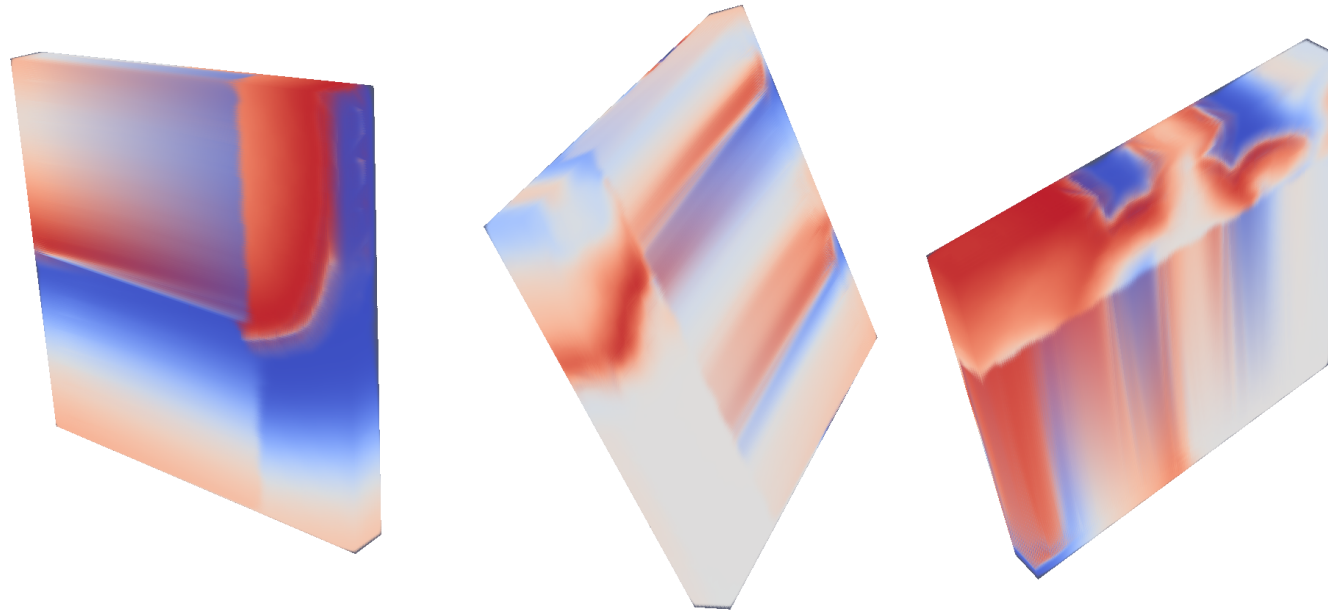
PHI vs GPU

KNL advantages:

- No heterogeneous programming
- Smaller penalty for exceeding 16 GB
- Could use MCDRAM <-> DDR swapping
- Low reuse: requires temporal blocking to be effective

Questions ?

A



B

